

Knowledge Progression in counting and place value, addition and subtraction

Number and P	lace Value							
Counting								
Three and Four- Year-Olds	our- Mathematics			 Recite number Say one number Know that the l total ('cardinal) 	 Recite numbers past 5. Say one number name for each item in order: 1, 2, 3, 4, 5. Know that the last number reached when counting a small set of objects tells you how many there are in total ('cardinal principle'). 			
Reception	Mathematic	cs		Count objects,Count beyond to	Count objects, actions and sounds.Count beyond ten.			
ELG-End of Reception Assessment	Mathematic	cs	Numerical Patterns	Verbally count	Verbally count beyond 20, recognising the pattern of the counting system.			
Year Grou	ıp	Ye	ear 1 Year 2 Year 3 Year 4 Year 5 Year 6			Year 6		
Counting •Count to and across 100, forwards and backwards, beginning with 0 or 1, or from any given number • • • • • • • • • • • • • • • • • • •		•Count in steps of 2 and 10, from any number, forward and backward •Count in multiples of 5	 Count from 0 in multiples of 3, 4, 6, 8, 50 and 100; Find 10 or 100 more or less than a given number bridging 100 	 Count in multiples of, 7, 9, 25 and 1000 Find 1000 more or less than a given number Count backwards through zero to include negative numbers Find the difference between two negative numbers 	•Count forwards or backwards in steps of powers of 10 for any given number up to 1 000 000 •Interpret negative numbers in context, count forwards and backwards with positive and negative whole numbers, including through zero • Find the difference between two numbers	 Use negative numbers in context, and calculate intervals across zero Add and subtract negative numbers 		

					including negative and	
					positive numbers	
Year 1 examples	Expected Compare amounts. What's the same? What's different? Children compare the bead strings and notice: One has 9 beads and the other has 6 beads. 9 is 3 more than 6. 6 is 3 less than 9. Pupils should be able to successfully respond to questions such as: Count forwards from 36, etc. Point to the third object in the line. Show me 8 cubes. Pupils should demonstrate one to one correspondence, cardinality and conservation of number.			Greater Depth I am going to count on from 20. Will I say the number 19? Convince me. I am going to count on in twos from 3. Will I say an even number? Convince me. I am going to count backwards from 20. How many steps will it take to reach 0? Convince me. I am going to count backwards in twos from 20. How many steps will it take to reach 0? Convince me.		
Year 2 examples	Working at Steve says, 'My number has two tens and five ones.' What is Steve's number? Amy has two more tens than Steve. What is her number? Sam says, 'My number has five tens.' What numbers can it be?			Greater depth 'When I count in tens from any number the units digit stays the same.' Do you agree? Explain your reasoning.		
Year 3 examples	<u>Working at</u> 392 + 10 =			$\frac{\text{Greater depth}}{995 + 100} = 4$	928 + 100 =	
Year 4 examples	What temperature is	5 degrees lower tha	ın -2 degrees Celsius?	The sea level is usually Look at the picture of the red fish is at -5 re Where is the yellow fish Where is the green fish Can you draw a fish at Can you draw a seagul level? What would the positive the seagull be if each of	r taken as zero. the lighthouse. n (5 metres below sea le sh? -35 m? I at 20 m above sea on of your fish and of the intervals on	evel):

							the lighthouse represented 7 m?		
							(NRICH)		
Year 5 examples	The temperature at 6 a.m. was recorded each day for one week. What was the coldest morning? What was the warmest morning? What is the difference in temperature between Monday and Tuesday?				Monday	ne / and	The temperature at 6 a.m. was recorded each day for one week.DayMTWTHFSATSUN1-1032-3-3What is the difference in temperature between the coldest day and		
	Place the record	ed temperatu	res in ord	der from	smallest	to	the warmest		
	Day M	T W	TH	F	SAT	SUN	At what time of year do you think these temperatures were		
	1	-1 0	3	2	-3	-3	recorded?		
							Do you think it might have snowed during the week? Explain your reasoning.		
Year 6 examples	A scientist measu	ures the dept	n of some	e objects	below t	he	A scientist measured the temperature each day for one week at		
	surface of the se	a.	c ucing n	ogativo r	umborg		06:00.		
		measurement	s using n	egative i	lumbers	•	On Monday the temperature had fallen by 3°C.		
	Object		depth				On Tuesday the temperature had fallen by 2·1°C.		
	Coral reef		-2				On Wednesday the temperature had risen by 1.6°C.		
	Shipwreck		-11				On Friday the temperature had fallen by 0.9° C.		
	Pirate treasure		four t	imes as o	deep as t	he	On Saturday the temperature had risen by 0.2°C.		
			coral	reef			What was the temperature on Saturday?		
	Sleeping shark		3 met shipw	res abov reck	e the				

	Is the sleeping shark	est? Explain your cho deeper than the pira	pice. Ite treasure? Explain			
	your reasoning.		•			
	A seagull is hovering	1 m above the surface	ce of the sea. How far			
	apart are the					
	seagull and the coral	reef?				
Place value and	•Recognise the place value of each digit in	•Recognise the place value of each	•Recognise the place value of each digit in a	•Read, write, order and compare numbers	•To be able to read, write, compare and	•Read, write, order and compare numbers
ronrosonting	a two-digit number	digit in a two -digit	three-digit number	up to 10 000 and	order any number to 1	up to 10 000 000 and
representing	 Identify and 	number	•Identify, represent	determine the value of	000 000 and determine	determine the value of
number	represent numbers	•identify, represent	and estimate numbers	each aigit •Identify represent	•Round any number	•Round any whole
	pictorial	numbers using	representations such	and estimate numbers	up to 1 000 000 to the	number to a required
	representations	different	as diennes	using different	nearest 10, 100, 1000,	degree of accuracy
	including the number	representations,		representations such	10 000 and 100 000	
	ten frames	number line	•Order and compare	•Round any number to	Read Roman numerals	
		diennes, and ten	•read and write	the nearest 10, 100 or	to 1000 (M) and	
	•Compare and order	frames	numbers up to 1000 in	1000	recognise years written	
	numbers from 0 up	•Compare and	numerals and in words	•Read Roman	in Roman numerals	
	• Use language of:	to 100 using <.>		C) and know that over	Roman numerals	
	equal to, more than,	and = signs		time,		
	less than (fewer),	 Read and write 		the numeral system		
	most, least	numbers to at least		changed to include the		
	• Read and write numbers from 1 to	and in words		place value		
	20 in numerals and					
	words					

Year 1	Expected	Greater Depth
examples	Write the numbers in order of size.	23456
examples	15 16 5 71 50	Use two of the digit cards to make a number greater than 50
	What is one more than ?	Use two of the digit cards to make a number less than 30.
	What is one less than ?	Use two of the digit cards to make an odd/even number.
	Complete:	Use two of the digit cards to make a number between 47 and 59.
	19 21.22.	What is the smallest 2-digit number you can make?
		What is the largest 2-digit number you can make?
		Explain your reasoning.
Year 2 examples	Working at	<u>Greater depth</u>
	Put a circle around the larger number.	Write all the 2-digit numbers greater than 40 using these digits.
	1) 50 48 2) 77 81 3) 78 87	2466
		How do you know you have them all? Prove it.
Year 3 examples	Working at	674 is made of 6 hundreds, 7 tens and 4 ones.
-	8 hundreds, 3 tens and 6 ones together make	674 is also made of 67 tens and 4 ones.
	457 is made of hundreds,tens and ones.	674 is also made of 6 hundreds and 74 ones.
	250 is made of hundreds and tens.	Find different ways of expressing:
		630
		704
		867
Year 4 examples	Working at	Greater Depth
	Match 4600 to numbers with the same value.	How many different ways can you write 5510?
	460 tens	Pupils should suggest answers such as:
	460 nundreas	551 tens
	46 nunareas	55 nunareas and 1 ten
	4600 Ones	5 thousands and 510 ones
	40 tens	
Year 5 examples	Working at	Greater depth
	What can we say about 48 000?	Using all of the digits from 0 to 9, write down a 10-digit number.
	It is less than 50 000.	What is the largest number you can write?

	It is made of 40 000	and toge	ther.	What is the smallest number you can write?		
	It is made of	thousands.		Write down the number that is one less than the largest number		
	It is made of	hundreds		Write down the number that is one more than the smallest number		
	It is made of	tons		(Using the digits 0 to 0 we can write		
		tens.		, Using the digits 0 to 9 we can write		
				any number, no matter now large or small.		
				Do you agree?		
				Explain your reasoning	<u>.</u>	
				Constants		
	<u>working at</u>			<u>Greater depth</u>		
	Estimate the answer	to 4243 + 1734 by ro	bunding the numbers	Three pupils are asked	to estimate the answer	to the sum 4243 +
	to:			1734.		
	the nearest 1000			Andrew says, 'To the n	earest 100, the answer	will be 5900.'
	the nearest 100			Bilal says, 'To the near	est 50, the answer will b	e 6000.'
	the nearest 50			Cheng says, 'To the ne	arest 10, the answer wil	l be 5970.'
	the nearest 10.			Do you agree with And	frew, Bilal or Cheng?	
				Can you explain their reasoning?		
Number facts		Number bonds	Number bonds	Number Bonds	•To be able to find	
	 Read, write and 	•Use place value	•To be able to	•To be able to	fractions and	
(+/-)	interpret	and number facts	calculate pairs of 2	calculate number	percentages of	
	mathematical	to solve problems	digit numbers which	bonds for 1000 (362 +	different amounts by	
	statements involving	recall and use	total 100 (36 + 64)	628)	Halving and doubling	
	addition (+),	addition and		•Number bonds to 1	20% of £15 = 10% of	
	subtraction (-) and	subtraction facts to		decimal place	£15 x 2	
	equals (=) signs	20 fluently, and	Doubling and halving	e.g.0.8 + 0.2	36 x 25 = 36 x 100 ÷ 4 =	
		derive and use		•All number bonds to 2	(36 ÷ 4) x 100	
	Number bonds	related facts up to	• <u>To be able to double</u>	decimal places	1.6 ÷ 2 = 0.8	
	 Represent and use 	100	and half all 2 digit and	<u>e.g. 0.12 + 0. 88</u>		
	number bonds and	e.g. All pairs of	numbers			
	related subtraction	multiples of 10 with	half of 36 is 18	Doubling and halving	Near doubles	
	<u>facts</u>	a total of 100	To be able to halve all		<u>421 + 387 is double</u>	
	<u>within 20</u>	<u>e.g. 30 + 70</u>	odd numbers to 10	• To be able to double	400 add 21 and then	
	•To know number	All pairs of	<u>e.g. half of 7 = 3.5</u>	and halve all 1,2 3 digit	subtract 13	
	bonds for 20	multiples of 5 with		odd and even		
	Demonstrate an	a total of 100	 To be able to double 	numbers by	 Near doubles 	
	understanding of	<u>e.g. 45+ 55</u>	and halve all multiples	partitioning or recall	<u>1.5 + 1.6 is double 1.5</u>	
	inverse +/-	 Recall and use 	<u>of 10 to 1000 e.g.</u>	<u>e.g.</u>	and add 0.1 or double	
	 Given a number, 	doubles and halves	half of 900 is 450	<u>346 x2 = 600 + 80 + 12</u>	1.6 and subtract 0.1	
	identify one more	to 20 To be able to		• <u>To be able to find a</u>		
	and one less	double all multiples		quarter of 3 digit		
	Doubling and halving	<u>of 10 to 100 (100+</u>	Near doubles	numbers by halving		
		<u>100)</u>	• <u>To know</u>	twice		

	•Doubles to 20	•To be able to half	38 + 35 is double 35			
	(10+10)	all even numbers	and add 3	• To be able to double		
	To be able to halve	to 20. •To be able		tenths numbers		
	even numbers to 20	to halve all		bridging 1		
		multiples of 10		e.g. 0.7 + 0.7		
	Near Doubles	Near doubles				
	To know	•To know		Near doubles		
	5 + 6 is double 5 and	13 + 14 is double 13		•160 + 170 is double		
	add 1 or double 6	and add 1		150 and add 10 then		
	and subtract 1	40 + 39 is double 40		add 20, or double 160		
		and subtract 1		<u>and add 10,</u>		
		<u>18 + 16 is double 18</u>		or double 170 and		
		and subtract 2 or		subtract 10		
		double 16 and add		<u>380 + 380 is double</u>		
		<u>2</u>		400 and subtract 20		
		<u>60 + 70 is double 60</u>		<u>twice</u>		
		and add 10 or				
		double 70 and				
		subtract 10				
Year 1 examples	Working at			<u>Greater depth</u>		
	Complete:			If you know one fact, w	what other facts do you	know?
	3 +? = 10 10 -? = 3	13 +? = 20 20 -? = 13		Complete:		
	? + 5 = 10 10 - 5 =?	15 +? = 20 20 - ? = 1	5	5		
	? +? = 10 10 -? =?	16 + ? = 20 20 - ? =	16	3+2		
	What do you notice?	?		10 -5		
	Children may 'know'	' number pairs totalliı	ng ten but are they			
	able to use them to					
	support other calcul	ations? For example,	when probed to say, 'If			
	vou know 3 + 7 = 10,	, ,	, , ,			
	what else do vou kno	ow?' They should rep	lv with answers. such			
	as 13 + 7 = 20 or 4 + 100 or 4 + 1	7	,			
	= 11	-				
Vear 2 examples	What do you notice	about each set of cal	culations?	Greater depth		
ical 2 champles	What's the same and	d what's different ab	out the three sets of	35 + ? = 100		
	calculations?			25 + ? = 100		
		20_10 - 1	00- 90-	45 + 2 = 100		
	10-9-	20-13 - 1	00- 90-	4J + : - 100		

	10 – 8 =	20 - 18 =	100-80 =	What do you notice ab	oout the ones digits in th	ese number sentences
	10 – 7 =	20 -17 =	100 -70=	?		
	10 – 6 =	20 -16 =	100 -60=	Can you explain why e	ach ones digit is a 5?	
Year 3 example	Working at			Greater depth		
	Near doubles			Near doubles		
	35 + 36 =			38 + 35 =		
	Double 35 + 1			Double 35 + 3		
Year 4 example	Working at			Greater depth		
•	Near doubles			Near doubles		
	<u>160 + 170 = 160 and a</u>	<u>dd 10,</u>		380 + 380 is double 400 a	and subtract 20 twice	
Year 5 example	Working at			Greater depth		
	<u>Doubles</u>			• <u>Near doubles</u>		
	1.5 + 1.5			<u>1.5 + 1.6 is double 1.5 and add 0.1</u>		
• •	Add and subtract	•Add and subtract	•Add and subtract	•Add and subtract	•Add and subtract	•Porform montal
Mental +/-	•Auu and subtract	•Aud and subtract	•Aud and subtract	•Aud and subtract	•Aud and subtract	calculations including
•	digit numbers to 20.	concrete objects.	including: HTU+U.	including bridging	increasingly large	with mixed operations
	including	pictorial	HTU+T	1000's	numbers	and large numbers
	zero	representations,	and HTU+H			
	 Understand the 	and mentally,	570 + 300 count on in	• <u>To be able to</u>	• <u>To be able to</u>	
	effect of adding and	including: TU+U,	hundreds from 300	partition using	mentally add and	
	subtracting 0	TU+T, TU+TU and	960 – 500 count back in	multiples of 10 and	subtract tenths, and	
	•Show that addition		or count on in hundreds	<u>100</u>	<u>one-digit whole</u>	
	be done in any order	<u>10 be able to</u>	from 500	$540 \pm 280 = 540 \pm 200$	<u>numbers and tenths</u>	
	(commutative) and	through multiples		<u>540 + 280 - 540 + 200</u> + 80		
	subtraction of one	of 10	To be able to partition	$\frac{1}{276} - 153 = 276 - 100$	0.8 + 0.35 = 0.8 + 0.2 +	
	number from	0110	using multiples of 10	<u> </u>	0.15	
	another	6+7=6+4+3				
	cannot	$\frac{23-9}{23-3-6}$	55 + 37 = 55 + 30 + 7	• <u>To be able to</u>		
	• <u>To be able to</u>	<u>15 + 7 = 15 + 5 + 2</u>	<u>= 85 + 7</u>	partition bridging		
	through multiples of		<u>43 + 28 + 51 = 40 + 20 +</u>	and through 1 when		
	10	• <u>To be able to</u>	$\frac{50+3+8+1}{2}$	adding decimals		
		count on 2 to 70		4400000000000000000000000000000000000		
	6 + 7 = 6 + 4 + 3	$\frac{\text{trien 3 to /3}}{99,73-69}$	• <u>IO DE ADIE TO</u>	<u>57 + 13 + 1</u>		
	<u>23 - 9 = 23 - 3 - 6</u>	<u>e.g. 75 - 00</u>	partition bridging			

	<u>15 + 7 = 15 + 5 + 2</u>	86 – 30 count back in tens from 86 or count on in tens	$\frac{\text{through multiples of}}{10}$ $\frac{49 + 32 = 49 + 1 + 31}{10}$	$\frac{3.8 + 2.6 = 3.8 + 0.2 +}{2.4}$ $\frac{5.6 + 3.5 = 5.6 + 0.4 +}{2.6 + 0.4 + 0.4 +}$		
		from 30 • To be able to partition using multiples of 10	• <u>Partitioning using</u> compensating	$\frac{3.1}{296 + 134 = 296 + 4 + 130}$		
		$\frac{30 + 47 = 30 + 40 + 7}{78 - 40 = 70 - 40 + 8}$ $\frac{25 + 14 = 20 + 5 + 10}{25 + 10}$	<u>84 – 19 = 84 – 20 + 1</u>	 Partitioning using compensating 38 + 69 = 38 + 70 - 1 		
		$\frac{+4}{=20+10+5+4}$ $\frac{23+45=40+5+20}{+3}$ $\frac{+3}{=40+20+5+3}$		$\frac{53 + 29 = 53 + 30 - 1}{64 - 19 = 64 - 20 + 1}$ $\frac{138 + 69 = 138 + 70 - 1}{138 + 100 - 1}$		
		$\frac{-40+20+3+3}{68-32=60+8-30}$ $\frac{-2}{=60-30+8-2}$				
		$\frac{Partitioning using}{compensating}$ $\frac{34 + 9 = 34 + 10 - 1}{2}$				
		$\frac{52+21=52+20+1}{70-9=70-10+1}$ $\frac{53+11=53+10+1}{53+10+1}$				
Year 1	Working at		I	Greater depth		
evamples	0 + 5 = 5 1 + - 5			I'm thinking of a numb What number was	er. I've subtracted 5 and	d the answer is 7.
examples	2 + = 5			I thinking of? Explain h	iow you know.	
	3 + = 5			I'm thinking of a numb	er. I've added 8 and the	answer is 19. What
	4 + = 5			thinking of? Explain ho	ow you know.	
	5 + = 5 Now do the same for rows of 6 counters 7 counters 8			I know that 7 and 3 is 2	10. How can I find 8 + 3?	How could you work
	counters, 9 counters and 10			It out?		
	counters.			If you add together six	Os the answer is 6.'	
	Children should be a 10. Exposing the	ble to recall all numb	er bonds to and within	Do you agree?		

	structure of the mathematics supports this process. They should	Explain your reasoning.
	then apply this to	
	number bonds to 20, so if 5+3 = 8, 15 +3 = 18	
	'If you add 0 to a number, the number	
	stays the same.'	
	Do you agree?	
	Explain your reasoning	
Veen 2 evenue	Working at	Greater depth
Year Z example	What do I need to add to or subtract from each of these	I think of a number and I add 2. The answer is 17. What was my
	numbers to total 60?	number?
	40, 44, 66, 69, 76, 86, 99, 89, 79,	I think of a number and I subtract 5. The answer is 24. What was my
	-, , -, -, -, -, -, -, -, -	number?
	Working at	Greater denth
Year 3 example	Write the four number facts that this har model shows	Flo and lim are answering a problem:
-		Danny has read 62 pages of the class book lack has read 43. How
	540	many more
	200 240	nary more has Danny road than lack?
	300 240	pages has Daminy read than Jack: Ele doos the calculation 62 \pm 42 lim doos the calculation 62 \pm 42
		When is correct?
		Explain how you know
		Explain now you know.
		Pupils might demonstrate using a bar model to explain their
	Moulting at	Teasoning.
Year 4 example	<u>working at</u>	Greater depth
•	Decide on a mental of written strategy for each of these	write three calculations where you would use mental calculation
	calculations and	strategies and three
		where you apply a column method.
	04 + 30 C40 + 2C0	Explain the decision you made for each calculation.
	640 + 360	
	64 + 79 + 36	
	3/8 + 502	
	8/6 + 9/1	
	999 + 999	
	144/+2362	
	1999 + 8/4	

	Write four number fa	acts that this bar diag	gram shows.	Use this number sentence to write down three more pairs of		
rear 5 example		9.5	<u>,</u>	decimal numbers		
	3.8		5.7	that sum to 3:		
		I		1.6 + 1.4 = 3		
Voar 6 ovamplo	Calculate 36·2 + 19·8			Jasmine and Kamal have been asked to work out 5748 + 893 and		
	with a formal writter	n column method		5748 – 893.		
	with a mental metho	od, explaining your re	asoning.	Jasmine says, '893 is 7 less than 900, and 900 is 100 less than 1000,		
				so I can work		
				out the addition by adding on 1000 and then taking away 100 and		
				then taking		
				away 7.	mina gat and is sha aan	ra at J
				Kamal says '893 is 7 le	initie get, and is she con	100 less than 1000 so
				I can work out	.35 than 500, and 500 is	100 1033 (11011 1000, 30
				the subtraction by taki	ng away 1000 and then	taking away 100 and
				then taking	0 1, 111	0 0, 1
				away 7.'		
				What answer does Kar	nal get, and is he correc	t?
				If you disagree with either Jasmine or Kamal, can you correct their		
				reasoning?		
				Write different number sentences using the digits 2, 3, 5 and 8		
	Compare 31 + 9 x 7 a	and $(31 + 9) \times 7$		before the equals		
	What's the same? W	hat's different?		sign. using:		
				one operation		
				two operations but no	brackets	
				two operations and br	ackets.	
Annaratus and	•Use objects to	•Use a number line	 Represent addition 			
	combine two parts	to count on/ back	and subtraction using			
informal	to make a whole or	•Dennesset	the part, part whole			
•••	subtract	•represent	model and the bar			
written	•Childron to	auullon	model			
mothods $\pm /$	roprosont the cubes	subtraction using	•Draw a number line			
methous +/-	represent the cubes	the part, part	to show adding and			
			subtracting a single			
			subtracting a single			

	using dots and	whole model and	digit to a two digit		
Reay strategy	crosses	the bar model	number bridging tens		
nrogression			e.g. 46 + 7 = 46 + 4 + 3		
progression	•Use part part	•Draw a number			
(in order)	whole model to	line to show	Partition a single digit		
(show addition/	adding and	number to add		
	subtraction	subtracting a single	without using a		
		digit to a two digit	number line		
	•Use a number line	number bridging			
	or Numicon to count	tens e.g. 46 + 7 =	•Draw a number line		
	on	46 + 4 + 3 and 54-6	and count in ten 's and		
	Represent addition	= 54 – 4= 50 -2 = 48	then multiples of 10 to		
	in a bar model which		add a two digit		
	encourages children	•Use a 100 grid to	number to a two digit		
	to count on rather	add/subtract a two	number and to		
	than count all	digit number to a	subtract a two digit		
		two digit number	number by ' counting		
	•Regrouping to	first	on ' to find the		
	<u>make 10</u>	adding/subtracting	difference		
	Using ten frames	tens and then ones	•Partition 3 digit		
	and counters/	•Add two two	numbers to add using		
	Numicon e.g. $6+5-6+4+1$ or	digit numbers	hase ten and		
	0+3=0+4+101	using hase ten	recording nictorially		
	$e.g. 14 - 3 - 14 - 4 - 10_{-1}$	renresenting the	hefore recording as		
	10-1	hase ten nictorially	number sentences		
	•Children to draw	e g lines for tens	number sentences		
	the ten frame and	and dots/ crosses	•Use base ten to		
	counters/ cubes	for ones then by	introduce the column		
		nartitioning into	method and carrying a		
	•Children to use	tens and ones to	ten over <mark>, children to</mark>		
	base 10 to add a	add	represent this		
	single digit to a two		pictorially		
	digit number and	•Partition two digit			
	develop their	numbers to	•Use the formal		
	understanding of	subtract e.g 56 – 24	method to add 2 and 3		
	place value	= 50 - 20 = 30 , 6 -			
		4 =2			

	•Children to	•Draw a number	digit numbers			
	represent this	line to subtract a	including carrying			
	pictorially	two digit number				
		from a two digit	•Use base ten to			
		number bridging	introduce the column			
		the tens e.g. 54 –	method for			
		26	subtraction and			
		- Deserve and the second	borrowing a ten ,			
		•Draw a number	this pictorially			
		tons to add a two	this pictorially			
		digit number to a	•Use the formal			
		two digit number	written method to			
			subtract 2, 2 digit			
		•Use base ten to	numbers including			
		introduce the	borrowing			
		column method				
		and carrying a ten				
		over, children to				
		represent this				
		pictorially				
VA/withow 1/		•Add two digit	 Add and subtract 	Add and subtract	 Add and subtract 	•Use formal methods
written +/-		numbers using the	numbers with up to	numbers with up to 4	whole numbers with	to add and subtract 5
		column method	three digits, using	digits using the formal	more than 4 digits,	digit numbers and
		supported	formal	written methods of	including using formal	beyond in different
		pictorially and with hase 10	columnar addition and	subtraction where	•Lise formal methods	contexts such as
		buse 10	subtraction	appropriate	to add and subtract	money and measures
					decimal numbers, up	
					to 2 decimal places	•Use formal methods
						to add and subtract
						to 3 decimal places
						to 5 decimal places

	Sam has completed t	hese calculations h	It he is incorrect	Greater depth		
Year 3 example	Sann nas completed t	has made				
• E	225	nas maue.		There are six 3-digit ad	Idition calculations show	vn below.
	⊃∠⊃ ⊾ 2/17			174		
+	581			+ 233		
				<u> </u>		
	355			579		
=	- 247			<u>+ 221</u>		
-	112					
				044 + 172		
				<u> </u>		
				791		
				+ 163		
				366		
				<u>+ 277</u>		
) 00/ + 233		
				<u> </u>		
				Which calculations hav	ve no carry digits?	
				Which calculations hav	e a carrying digit only o	nce?
				Which calculations hav	ve a carrying digit twice?	?
				Which calculation has	the largest answer?	
				Which calculation has	the smallest answer?	
				Check that children are	e looking at the numbers	s involved, rather than
				doing the		,
				calculations.		
				-		
Money	Recognise and	 Recognise and use 	 Add and subtract 	•estimate, compare		
k k	know the value of	symbols for pounds	amounts of money to	and calculate different		
d	different	(£) and pence (p);	give change, using	measures, including		
d	denominations of	combine	both £ and p in	money in pounds and		
С	coins	amounts to make a	practical contexts	pence		
a	Find different	Find different		• Add and		
-	combinations of	combinations of	 To be able to find 	Auu allu subtract		
			change using montal	Subliace		
	coins that equal the	coins that equal the	change using memai	amounts of		

	same amounts of money •solve simple problems in a practical context including giving change to 20p and beyond	same amounts of money •Solve simple problems in a practical context involving addition and subtraction of money of the same unit, including giving change to £1 and beyond	methods and column subtraction	totals and give change selecting the most efficient method to complete the calculation		
Year 1	Working at			Greater depth		
examples	Show 19p using only 2p, 5p and 10p coins. Find three different ways to do it. Ali buys 3 bags of apples. Each bag has 4 apples in it. How many apples does he buy?			Using only 2p, 5p and 3 In how many different Are you sure you have Explain how you know Lollies cost 5p each. A pack of 3 lollies costs How much money do y instead of 3 single lollies?	10p coins, can you show ways can you do this? got them all? s 13p. you save when you buy a	[,] 20p? a pack of 3 lollies
Year 2	Working at			<u>Greater depth</u>		
examples	Grace uses a £1 coin to buy a can of drink which costs 80p. She is given three coins in change. What coins could she have been given?		Grace uses a £2 coin to buy a can of drink which costs 85p. She is given four coins in change. Find all the possible combinations of coins she could have been given.			

Year 3 examples	Working£2.60 + = £5.00If I buy a sandwich for £2.20 and a drink for 90p, how much change do I get from £5?Ellie buys 2 pencils. She pays with a £2 coin and gets 70p change. 	Greater depth Sophie and Ravi have saved some money. Altogether they have saved £35. Sophie has saved £4 more than Ravi. How much have they each saved? Sam and Tom share this money equally. Divide the coins into two equal groups. Could three friends share the money equally? Explain your reasoning.
		20p.20p,20p,50p,10p, 5p 5p
Year 4 examples	Working at Which would you rather have, 3 × 50p coins or 7 × 20p coins? Explain your reasoning.	Great depth Sid and Sam share some money. Sid gets twice as much as Sam. Tick the coins which Sid might take 50p, 20p, 20p,10p, 10p, 5p, 5p, Is there more than one way of sharing the coins?
Year 5	Mo has £1,000 to spend. He buys a TV and a games console. Does Mo have enough money left to buy the phone? Show your workings. TV - £349 Phone -£479 Games console - £199	

Year 6	A shop sells boxes of chocolates. One box costs £3.99. A second box costs £2.60 . A third box costs £6.45 . What is the difference in price between the most and least expensive boxes? The shop also sells packets of sweets. One packet costs £1.39 . Ramesh has a £10 note and he wants to buy the chocolates costing £2.60 . How many packets of sweets can he also buy?			A shop sells boxes of chocolates costing £2.60 . The shop also sells packets of sweets. One packet costs £1.39 . Ramesh has a £10 note and he wants to buy one box of chocolates. Sara says that Ramesh can work out how many packets of sweets he can buy using the number sentence 10 – 2.60 ÷ 1.39 . Do you agree or disagree with Sara? If you disagree, what number sentence do you think Ramesh should use? Explain your reasoning.		
Problems +/-	 Solve one-step problems that involve addition and subtraction, using concrete objects and pictorial representations, and missing number problems such as 7 = □ - 9 	 Solve problems with addition and subtraction, using concrete, pictorial and abstract representations Recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems. Solve missing number problems using addition and subtraction 	•Estimate the answer to a calculation and use inverse operations to check answers •Solve problems, including missing number problems, using number facts, place value, and more complex addition and subtraction	•Estimate and use inverse operations to check answers to a calculation •Solve addition and subtraction two-step problems in contexts, deciding which operations and methods to use and why	 Use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy should an answer include a decimal or fraction Solve addition and subtraction multi-step problems in contexts including money. Estimate. Decide which operations to use and why- 4 digit numbers and above, use formal written methods Solve problems using Roman Numerals and 	 Solve addition and subtraction multi-step problems with increasing difficulty in contexts, deciding which operations and methods to use and why Use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy.

					convert between the two	
Year 1 examples	Expected Use the first number sentence. 4 + 3 = ? 7 - ? = 4	ence to complet	te the second number	Greater Depth Write a pair of number ? + ? = 12 And another pair, and Can you find all possib	rs in the boxes to add to another, and another. ilities?	12.
	Robert has 5 more cherries than John. John has 11 cherries. How many does Robert have? Write a number sentence you would use to solve the problem.			Together Sam and Tom have 19 football stickers. Tom has 8 stickers. How many stickers does Sam have? Write a number sentence you could use to solve the problem.		
Year 2 examples	Write a number sentence you would use to solve the problem.Dan needs 80 g of sugar for his recipe. There are 45 g left in the bag. How much more does he need to get?The temperature was 26 degrees in the morning and 11 degrees colder in the evening. What was the temperature in the evening? A tub contains 24 coins. Saj takes 5 coins. Joss takes 10 coins. How many coins are left in the tub?			Together Jack and Sam have £12. Jack has £2 more than Sam. How much money does Sam have? A bar model can be very helpful in solving these types of problems. Jack +£2 altogether Sam and Jack = £12 Sam f12 - f2 = f10 $f10 \div 2 = f5$ Sam has £5		
Year 3 examples	Teddy has worked out an What subtraction could T	addition. 175 + eddy do to chec	135 = 300 :k he is correct?	Use the digit cards to r 3 4 5 6 7 8 Write an addition using What is the answer to addition. Talk about th	nake two 3-digit numbe g your numbers. your addition? Ask a pa le different methods you	rrs. artner to check your u can use.

Year 4 examples	Filip is working out 607 + 395	Tom is estimating to work out an addition.
	He rounds his numbers to the nearest 100 to estimate the	His estimate is 3,000 + 1,000 = 4,000
	answer.	Write three possible additions Tom could be working out.
	Complete the sentences.	
	607 rounded to the nearest 100 is	
	395 rounded to the nearest 100 is	
	Filip's estimate for the answer is	
Year 5 examples	Eva is reading a book before bedtime. On Monday she reads 38	Two numbers have a difference of 1,200 and a total of 6,484 What
	pages. On Tuesday she reads 6 pages more than she did on	are the two numbers?
	Monday.	
	How many pages does she read on Tuesday?	
	How many pages does she read altogether on Monday and	
	Tuesday?	
	There are 123 pages in the book altogether. How many pages	
	does Eva have left to read?	
Year 6 examples	A shop sells magazines and comics. Freya buys a magazine and	A shop sells magazines and comics. Last week Arthur bought a
•	a comic. She pays	magazine and
	£2.50 . Evie buys a magazine and two comics. She pays £3.90 .	a comic. He can't remember exactly what he paid, but he thinks he
	How much does a comic cost? How much does a magazine	paid £1·76 .
	cost?	Yesterday he bought a magazine and four comics. He paid ± 4.30 .
		Do you think he is remembering correctly when he says that he paid
		£1·76
		last week?

New vocabulary for each year group is in bold	Progression in vocabulary – Counting, number, addition and subtraction				
	Number	Place Value	Estimating	Addition and Subtraction	
EYFS	Zero , number, one, two, three to twenty and beyond, teens numbers, eleven, twelve twenty, none, how many? count, count (up) to, count on (from, to), count back (from, to)	Digit, the same number as, as many as more, larger, bigger, greater, fewer, smaller, less fewest, smallest, least, most, biggest, largest, greatest, one more, one less, compare, order	Guess, how many? Estimate, nearly, close to, about the same as, just over, just under too many, too few, enough, not enough	Add, more, sum, total, altogether, double, one more, two more how many more to make? how many more is than? how much more is? take away, how many are	

Year 1	is the same as, more, less, odd, even, few, pattern, pair Number, numeral , one, two, three twenty, teens numbers, eleven, twelve twenty, twenty-one, twenty- two one hundred, none, how many? count, count (up) to,	first, second, third twentieth last, before, after, next between Ones, tens, digit, the same number as, as many as, more, larger, bigger, greater, fewer, smaller, less, fewest, smallest, least, most, biggest, largest, greatest, one more, ten more	Guess, how many? estimate nearly, roughly , close to, about the same as, just over, just under, too many, too few enough, not enough	left/left over? how many have gone? one less, two less, how many fewer is than? how much less is? difference between Addition, add, more, make, sum, total, altogether, double near double, half, halve one more, two more ten more how many more to make? how many more is than?
	count on (from, to), count back (from, to) forwards, backwards, count in ones, twos, fives, tens equal to, equivalent to , is the same as, more, less ,most, least, many ,odd, even, multiple of, few, pattern, continue , pair	one less, ten less , equal to, compare, order, size, first, second, third twentieth, last, before, after, next, between half-way between , above, below		how much more is? Subtract, take away, how many are left/left over? how many have gone? one less, two less, ten less how many fewer is than? how much less is? difference between, equals, is the same as, number bonds/pairs/ facts, missing number, inverse
Year 2	Number, numeral, zero one, two, three twenty, teens numbers, eleven, twelve twenty, twenty-one, twenty- two one hundred, two hundred , none how many? count, count (up) to, count on (from, to), count back (from, to) forwards, backwards, count in ones, twos, fives, tens, threes , and so on, equal to, equivalent to, is the same as more, less most, least tally many odd, even, multiple of, sequence continue, predict , few, pattern	Ones, tens, hundreds, digit one-, two- or three-digit number place, place value stands for, represents, exchange, the same number as, as many as more, larger, bigger, greater fewer, smaller, less fewest, smallest, least, most, biggest, largest, greatest, one more, ten more, one less, ten less, equal to, compare, order, size, first, second, third twentieth, twenty-first, twenty-second last, before,	Guess, how many? estimate nearly, roughly ,close to, about the same as, just over, just under, exact, exactly	Addition, add, more, make, sum, total, altogether, double, near double, half, halve one more, two more ten more one hundred more, how many more to make? how many more is than? how much more is? subtract take away how many are left/left over? how many have gone? one less, two less, ten less one hundred less how many fewer is than? how much less is? difference between, equals, is the same

	pair, rule > greater than < less	after, next, between, halfway,		as, number bonds/pairs/facts,
				inverse, carry
Year 3	Number, numeral, zero, one, two, three twenty, teens numbers, eleven, twelve twenty, twenty-one, twenty- two one hundred, two hundred one thousand , none how many? count, count (up) to, count on (from, to), count back (from, to) forwards, backwards, count in ones, twos, fives, tens, threes, fours , eights, fifties and twenty five to hundreds equal to, equivalent to is the same as more, less most, least tally many odd, even, multiple of, sequence, continue, predict, few, pattern, pair, rule, relationship > greater than < less than, consecutive exact, exactly, too many, too few, enough, not enough, ascending/descending order	Ones, tens, hundreds digit one-, two- or three-digit number place, place value stands for, represents, exchange, the same number as, as many as more, larger, bigger, greater fewer, smaller, less fewest, smallest, least most, biggest, largest, greatest one more, ten more, one hundred more, one less, ten less, one hundred less, tenths, efficient method	Guess how many? estimate nearly, roughly, close to approximate, approximately about the same as, just over, just under	Addition, add, more, and make, sum, total, altogether, double, near double, half, halve, one more, two more ten more one hundred more, how many more to make? how many more is than? how much more is? Subtract, take away, how many are left/left over? how many have gone? one less, two less, ten less one hundred less ,how many fewer is than? How much less is ? Difference between, equals, is the same as, number bonds/pairs/facts, missing number, inverse, column addition and subtraction; carry, borrow
Year 4	Number, numeral, zero, one, two, three twenty, teens numbers, eleven, twelve twenty, twenty-one, twenty- two one hundred, two hundred one thousand ten thousand, none, how many? count, count (up) to, count on (from, to), count back (from, to) forwards, backwards, count in ones, twos, fives, tens, threes,	Ones ,tens, hundreds, thousands, digit one-, two- or three-, four - digit number, place, place value, stands for, represents, exchange, the same number as, as many as more, larger, bigger, greater, fewer, smaller, less fewest, smallest, least most, biggest, largest, greatest, one more, ten more, one hundred more, one	Guess ,how many, estimate nearly, roughly, close to, approximate, approximately, about the same as, just over, just under, exact, exactly, too many, too few, enough, not enough, round, nearest, round to the nearest ten, hundred, thousand, round up, round down	Addition, add, more, make, sum, total, altogether, double near double, half, halve, one more, two more ten more one hundred moreone thousand more, how many more to make? how many more is than? how much more is? Subtract, take away how many are left/left over? how many have gone? one less,

	sevens, nines, elevens, twelves, twenty-fives and so on to hundreds, thousands, equal to, equivalent to, is the same as, more, less most, least, tally, many, odd, even multiple of, factor of, sequence, continue, predict, few, pattern, pair, rule, relationship, next, consecutive > greater than < less than, ascending/descending order positive, negative above /below zero, minus negative numbers, square number, Roman numeral,	less, one hundred less, one thousand less, equal to compare, order, size, first, second, third twentieth twenty-first, twenty-second last, before, after, next, between halfway between above, below, tenths, hundredths, efficient written method		hundred less, one thousand less, how many fewer is than ? how much less is ?difference, between, equals is the same as, number bonds/pairs/facts missing , Column addition and subtraction; carry, borrow
Year 5	Number, numeral, zero, one, two, three twenty, teens numbers, eleven, twelve twenty, twenty-one, twenty- two one hundred, two hundred one thousand ten thousand, hundred thousand, million, none, how many? count, count (up) to, count on (from, to), count back (from, to) forwards, backwards count in ones, twos, fives, tens, threes, fours, eights, fifties, sixes, sevens, nines, twenty-fives and so on to hundreds/ thousands, equal to, equivalent to, is the same as, more, less, most, least tally, many ,odd, even multiple of, factor of ,factor pair	Ones, tens, hundreds, digit one- , two- or three-digit number place, place value, stands for, represents, exchange, the same number as, as many as, more, larger, bigger, greater, fewer, smaller, less, fewest, smallest, least, most, biggest, largest, greatest, one more, ten more, one hundred more, one thousand more, one less, ten less, one hundred less, one thousand less, equal to, compare, order, size, first, second, third twentieth twenty-first, twenty-second last, last but one, how many have gone? one less, two less, ten less one hundred less	Guess, how many? estimate, nearly, roughly, close to, approximate, approximately, about the same as, just over, just under, exact, exactly too many, too few, enough, not enough, round, nearest, round to the nearest ten, hundred, thousand, ten thousand, round up, round down	Addition, add, more, and make, sum, total, altogether, double, near double, half, halve, one more, two more ten more one hundred more, how many more to make? how many more is than? how much more is? subtract ,take away how many are left/left over? how many have gone? one less, two less, ten less one hundred less, how many fewer is than? how much less is ? difference between, equals, is the same as, number bonds/pairs/facts, missing number, inverse, Column addition and subtraction; carry, borrow

	sequence, continue, predict, few, pattern, pair, rule relationship, before, after, next between, halfway between, above, below next, consecutive > greater than < less than or equal to, Roman numerals integer, positive, negative above/below zero, minus, negative numbers, formula divisibility, square number prime number, ascending/descending order	how many fewer is than? how much less is? difference between, equals, is the same as, number bonds/pairs/facts, missing number, inverse, tenths, hundredths, thousandths		
Year 6	Number, numeral , zero, one, two, three twenty teens numbers, eleven, twelve twenty, twenty-one, twenty- two one hundred, two hundred one thousand ten thousand, hundred thousand, million, none, how many? count, count (up) to, count on (from, to), count back (from, to) forwards, backwards, count in ones, twos, fives, tens, threes, fours, eights, fifties, sixes, sevens, nines, twenty-fives and so on to hundreds/ thousands, equal to, equivalent to, is the same as more, less most, least, tally, many, odd, even ,multiple of factor of factor pair	Ones tens, hundreds, digit, one- two- or three-digit number place, place value, stands for, represents, exchange, the same number as, as many as more, larger, bigger, greater, fewer, smaller, less fewest, smallest, least most, biggest, largest, greatest, one more, ten more, one hundred more, one thousand more, one less, ten less, one hundred less, one thousand less, equal to ,compare ,order, size, first, second, third twentieth twenty-first, twenty-second last, last but one before, after next between, difference between equals is the same	Guess, how many? estimate, nearly, roughly, close to, approximate, approximately, about the same as, just over, just under, exact, exactly too many, too few enough, not enough round, nearest, round to the nearest ten, hundred, thousand, ten thousand, round up, round down	Addition, add, more, make, sum, total, altogether, double near double, half, halve one more, two more ten more one hundred more, how many more to make? how many more is than? how much more is? Subtract, take away how many are left/left over? how many have gone? one less, two less, ten less one hundred less, how many fewer is than? how much less is ? Difference between, equals, is the same as, number bonds/pairs/facts missing number ,inverse, Order of operations, Column addition and subtraction: carry, borrow

sequence, continue, predict,	as, number bonds/pairs/facts	
few, pattern, pair, rule,	missing number, tenths	
relationship, next, consecutive		
> greater than < less than,		
halfway between, above,		
below,		
\geq greater than or equal to, \leq		
less than or equal to, Roman		
numerals integer, positive,		
negative, above/below zero,		
minus, negative numbers,		
formula, divisibility, square		
number, prime number,		
factorize, prime factor		
ascending/descending order,		
digit, total		

	Vocabulary progression – Money and problem	
	solving	
	Money	Problem solving
EYFS	Money ,coin, penny, pence, pound ,price, cost buy, sell spend, spent	Pattern, puzzle , what could we try next? How did you work it out?
	рау	recognise ,describe, draw, compare, sort
Year 1	Money, coin, penny, pence, pound price, cost buy, sell spend, spent,	Pattern, puzzle problem, problem solving, mental, mentally, what
	pay, change, dear, costs more, cheap, costs less, cheaper, costs the	could we try next? How did you work it out? explain your thinking,
	same as how much? How many? total	recognise, describe, draw, compare, sort
Year 2	Money, coin, penny, pence, pound price, cost buy, bought, sell, sold	Pattern, puzzle problem, problem solving mental, mentally what could
	spend, spent, pay change, dear, costs more, cheap, costs less,	we try next? How did you work it out? show how you explain your
	cheaper costs the same as how much? How many? total	thinking
Year 3	Money, coin, penny, pence, pound, price, cost buy, bought, sell, sold	Pattern, puzzle, problem, problem-solving mental, mentally, what could
	spend, spent pay change, dear, costs more, cheap, costs less,	we try next? How did you work it out? show how you explain your
	cheaper costs the same as how much? How many? total	thinking, explain your method describe the pattern, describe the rule,
		investigate, recognise describe, draw, compare, sort greatest value,

		least value mental calculation, written calculation, statement, explain
		your reasoning
Year 4	Money, coin, penny, pence, pound, price, cost buy, bought, sell, sold	Pattern, puzzle, problem, problem, solving mental, mentally, what
	spend, spent pay change, dear, costs more, cheap, costs less,	could we try next? How did you work it out?
	cheaper costs the same as how much? How many? total	explain your reasoning
Year 5	money ,coin, penny, pence, pound price, cost buy, bought, sell, sold	Pattern, puzzle, problem, problem solving, mental, mentally, what
	spend, spent pay change dear, costs more cheap, costs less, cheaper	could we try next? How did you work it out? show how you explain
	costs the same as how much? How many? total discount	your thinking, explain your method, describe the pattern, describe the
	currency	rule, investigate, recognise, describe, draw, compare, sort greatest
		value, least value, mental calculation, written calculation, statement,
		justify, make a statement, explain your reasoning
Year 6	money ,coin, penny, pence, pound price, cost buy, bought, sell, sold	Pattern, puzzle, problem, problem solving mental, mentally what could
	spend, spent pay change dear, costs more cheap, costs less, cheaper	we try next? How did you work it out? Show how you explain your
	costs the same as how much? How many? total discount	thinking explain your method, describe the pattern, describe the rule,
	currency, profit, loss	investigate, recognise, describe, draw, compare, sort, greatest value,
		least value, mental calculation, written calculation, statement, justify,
		make a statement, explain your reasoning